CALIFORNIA STATE UNIVERSITY, NORTHRIDGE

Performance Optimization in Computational Fluid Dynamics with Parallelism for Linear System Solvers

A thesis submitted in partial fulfilment of the requirements

For the degree of Master of Science in Mechanical Engineering

By

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Abstract

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Abstract text here…

# Introduction

Since the 1960s, Computational Fluid Dynamics (CFD) has been a tool implemented by scientists and engineers to solve a variety of complex problems related to fluid flow, heat and mass transfer, chemical reactions, and related phenomena [Versteeg 2007]. The aerospace industry was an early adopter of CFD, primarily using the technology to study the effects of drag and lift on aerodynamic bodies. Aircraft manufacturers like Airbus, Boeing, and Lockheed Martin, typically spend millions of dollars creating prototype aircraft to study the effects of fluid flow around the designed aircraft body [need a ref here]. By introducing a tool like CFD, aircraft manufacturers are able to filter out potential design flaws prior to actually manufacturing any form of aerodynamic body. As CFD has matured as a standard technology, it (CFD) has even replaced the need to physically test the aerodynamic effect of new aircraft designs [reference Boeing 787 design].

In performance racing, the use of CFD has become so integrated in the design process that every F1 car manufacturer / performance team has a dedicated CFD department. Furthermore, the use of CFD has expanded past simply modeling aerodynamic effects it now encompasses energy efficiency predictions in the combustion engines of.

# Objective

The scope of this study is to provide a framework for improving the computational performance of legacy CFD code, perform an optimization study of the current solutions to CFD problems, and determine the costs associated with implementing new technologies in legacy CFD code. The framework for improving the computational performance of legacy CFD code considers two classes of examples. The first class of examples, considers simple diffusion problems solved using the finite volume method and the centralized differencing scheme. This class of example is primarily used due to its simplicity as implementing parallelism on a simple problem provide a higher adherence of understanding when compared to a problem with increased complexity. The second class of examples focused on a two-phase flow boiling problem that incorporates a solution to the full, incompressible Navier-Stokes equations. This example is used to demonstrate the effectiveness of implementing parallelism in a complex, CFD problem.

The optimization study considers the rate of convergence for the solutions to sparse linear systems, the computational resource requirement for different solutions to sparse linear systems, and the duration of computation for given solutions on a variety of hardware platforms. The study also considers different means of implementation for each solution algorithm and how that implementation affects the performance metrics of the optimization study. The optimization study considers the same two classes of CFD problems as mentioned previously and considers cases for a 1-dimensional, 2-dimensional, and 3-dimensional environment.

Finally, the determination of cost associated with implementing each particular CFD solution is examined for both the simple diffusion problem and the two-phase boiling problem. The performance indications of cost are considered for the 1-dimensional, 2-dimensional, and 3-dimensional environments and assess the required revision and restructuring of legacy code necessary to implement new solution types.

# Mathematics

Computational Fluid Dynamics

Linear Algebraic Solvers

Parallel Solution Methods

# Numerical Model

Algorithm Study

Diffusion

Two-phase flow boiling

# Results

**One-Dimensional Diffusion**

A one-dimensional diffusion problem was solved with a heat flux boundary condition applied to the west side and a constant temperature boundary condition applied to the east side.

**Two-Dimensional Diffusion**

A two-dimensional diffusion problem was solved with a constant temperature boundary condition and a constant heat flux boundary condition. The constant temperature was applied to the north side of a two-dimensional grid and given a temperature of 100 °C. The heat flux boundary condition was applied to the west wall and given a heat flux of 500 W/m2. The nodal mesh was generated as a square and the number of nodes was varied from 10 to 100 in increments of 10 (i.e. 10, 20, 30, …100).

< figure of BC step up >

The following linear system solution algorithms were each used to solve the system of equations using the MATLAB scripting environment as well as in compiled FORTRAN:

* Tri-diagonal matrix algorithm (TDMA)
* Biconjugate Gradients (BiCG)
* Biconjugate Gradients Stabilized (BiCGStab)
* General Minimum Residual (GMRES)
* Pardiso (Intel MKL)
* MLDIVIDE (MATLAB)

For small grid sizes, the TDMA performed nearly as well as the Pardiso and MLDIVIDE algorithms. As the grid sizes increased, however, the TDMA convergence time significantly increased. For all solution algorithms, the compiled FORTRAN environment achieved the lowest time of convergence, with the Intel MKL Pardiso algorithm outperforming the others be a factor of 1.4 times.

< figure results >

With Jacobi-preconditioning applied to each of the algorithms (aside from the TDMA), the results are slightly improved for both the MATLAB and FORTRAN environments.

< figure results with jacobi >

With Incomplete LU-Decomposition (ILU), the convergence rates for BiCGStab and GMRES are nearly identical to the rates of convergence for the Intel MKL Pardiso and MATALB MLDIVIDE algorithms.

< figure results with ilu >

From the results of the two-dimensional case, it appears that the MLDIVIDE and Intel MKL Pardiso algorithms are optimized for near-symmetric matrcies. This agrees with the wide-spread uses of these algorithms in typical commercial software packages such as ANSYS, NASTRAN, and COMSOL.

**Three-Dimensional Diffusion**

A three-dimensional diffusion problem was solved in a similar configuration to the three-dimensional problem. A constant temperature condition was applied to the north wall and a heat flux boundary condition was applied to the west wall. The values for these boundary conditions were the same as in the two-dimensional problem, 100 °C and 500 W/m2. Additionally, the nodal mesh was kept in a cubic configuration with m, n, and l all having the same number of nodes. These values were varied from 10 to 400 with intervals of 10 until 100 nodes per side, then in intervals of 100 to 400 nodes per side.

< figure of BC setup >

The following linear system solution algorithms were each used to solve the system of equations using the MATLAB scripting environment as well as in compiled FORTRAN:

* Tri-diagonal matrix algorithm (TDMA)
* Biconjugate Gradients (BiCG)
* Biconjugate Gradients Stabilized (BiCGStab)
* General Minimum Residual (GMRES)
* Pardiso (Intel MKL)
* MLDIVIDE (MATLAB)

Each of the tested algorithms performed significantly faster than the TDMA for all cases when considering the number of iterations and computational run time. The Pardiso and MLDIVIDE algorithms were also significantly slower than the biconjugate gradient stabilized method as the number of nodes increased.

< figure results >

With Jacobi-preconditioning applied to each of the algorithms (aside from the TDMA), the results are slightly improved for BiCGStab and GMRES.

< figure results with jacobi >

With ILU preconditioning, the convergence rates for BiCGStab and GMRES perform significantly better than the Intel Pardiso and MLDIVIDE algorithm.

< figure results with ILU >

From the results of the three-dimensional case, it appears that the MLDIVIDE and Intel MKL Pardiso algorithms not optimized for matrices that are not symmetric.

# Conclusion

References